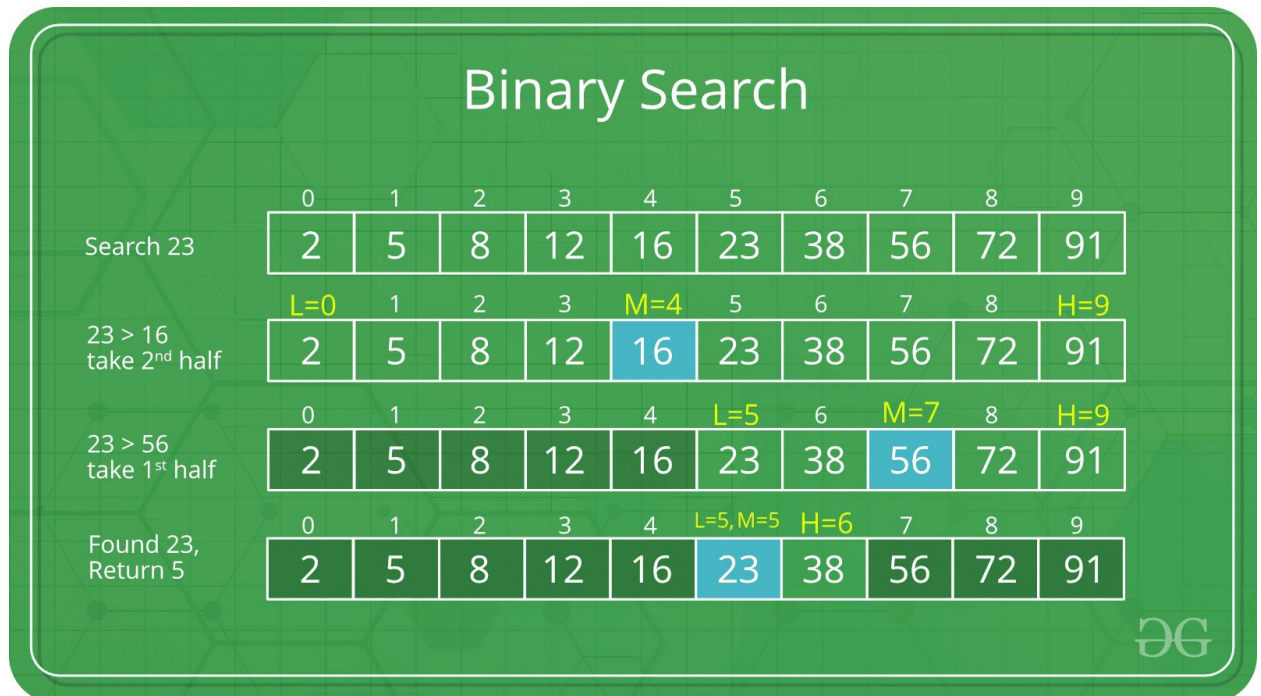


Binary Search :



Complexity : Time & Space

Calculating Time complexity:

- Let say the iteration in Binary Search terminates after **k** iterations. In the above example, it terminates after 3 iterations, so **here k = 3**
- At each iteration, the array is divided by half. So let's say the length of array at any iteration is **n**

- **At Iteration 1,**
Length of array = n
- **At Iteration 2,**
Length of array = $n/2$
- **At Iteration 3,**
Length of array = $(n/2)/2 = n/2^2$
- **Therefore, after Iteration k,**
Length of array = $n/2^k$
- **Also, we know that after**
After k divisions, the **length of array becomes 1**

Therefore

$$\text{Length of array} = n/2^k = 1$$

$$\Rightarrow n = 2^k$$

○

Applying log function on both sides:

$$\Rightarrow \log_2 (n) = \log_2 (2^k)$$

$$\Rightarrow \log_2 (n) = k \log_2 (2)$$

○

As $(\log_a (a) = 1)$

Therefore,

$$\Rightarrow k = \log_2 (n)$$

○

Hence, the time complexity of Binary Search is
 $\log_2 (n)$

Nested-loop complexity :

```

for(i=0; i<n; i++)
{
    for(j=0; j<n; j++)
    {
        for(k=0; k<n; k++)
        {
        }
    }
}

```

i=0, j=0,1,2...n-1
j=0; k=0,.....n-1
....
i=1, j=0,1,2...n-1
....
i=n-1, j=0,1,.....n-1

n=5, 5*5*5=125

Complexity : big_o(n^2)

Big_o -> Growth Function

$2x^3 + x^2 + 3x$

Complexity = max(power) = big_o(x^3)

Suppose , nested loop of i,j,k; complexity = 2 * big_o(n^3)

Nested loop i,j ; complexity = big_o(n^2)

loop of i ; complexity = 3 * big_o(n)